

Find the product of the last two digits of the number

$$2 \cdot 2^2 \cdot 2^3 \cdot 2^4 \dots 2^{999} \cdot 2^{1,000}.$$

Deadline for solution: 03/09/09.